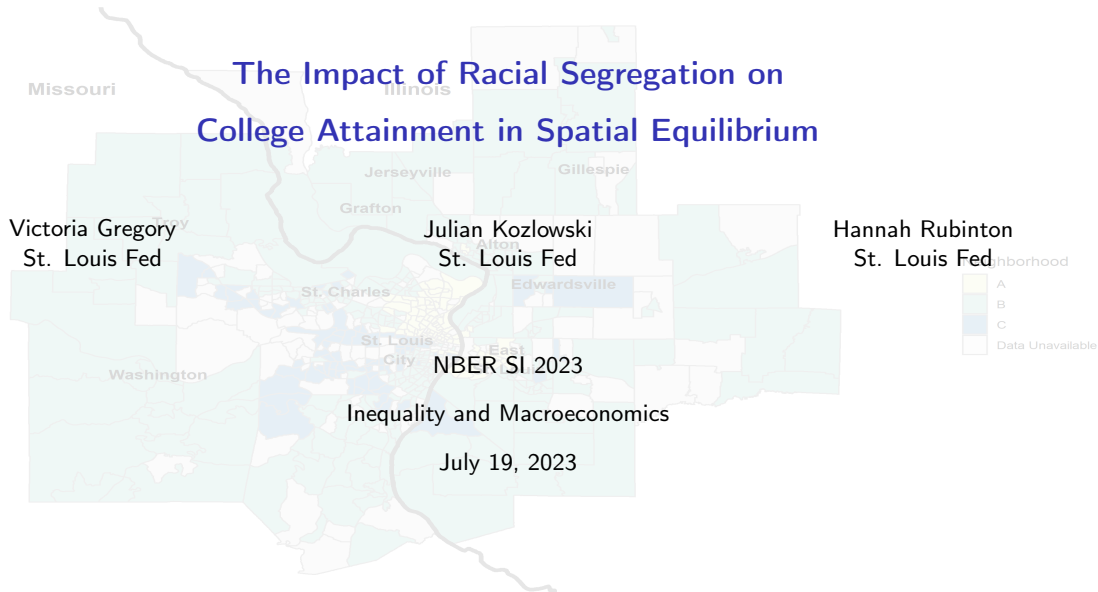


# The Impact of Racial Segregation on College Attainment in Spatial Equilibrium

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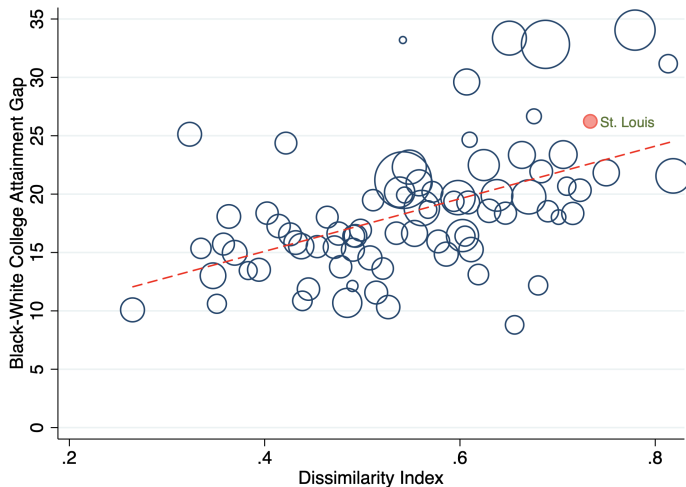
*The views expressed herein are solely those of the authors and do not necessarily reflect the views of the Federal Reserve Bank of St. Louis or the Federal Reserve System.*

## Black-White College Gap and Racial Segregation

- ▶ Large literature arguing that a child's **neighborhood** matters for their adult outcomes
- ▶ Racial and economic **segregation** are predominant features of many American cities
- ▶ **Racial inequality** in exposure to “high quality” neighborhoods (Bayer et al., 2021)

*Do racial differences in exposure to high-quality neighborhoods explain the Black-White college gap?*

## Black-White College Gap and Segregation



### In St. Louis:

- ▶ 47% of White children graduate from college
- ▶ 19% of Black children graduate from college
- ▶ 28 p.p. college gap

## Spatial Equilibrium and Race

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- ▶ Spatial equilibrium model of a city with racial differences:
  1. Black-White wage gap  
Gap in lifetime earnings between Black and White households
  2. Amenity externalities: households care about the racial composition of neighbors  
Fear of discrimination in all White neighborhood, White flight, homophily
  3. Moving costs vary by race  
Differences in borrowing constraints, discrimination in housing markets, information frictions

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Differences in borrowing constraints, discrimination in housing markets, information frictions
- ▶ General equilibrium neighborhood effects:
  - ▶ Rental markets
  - ▶ Human capital spillovers  
Peer effects, networks, school quality
  - ▶ Racial composition  
Matters due to amenity externalities

## The Impact of Segregation on Racial Gap in College Attainment

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- ▶ Model explains 80% of Black-White college gap and the level of segregation in St. Louis
  - ▶ The wage gap has a direct effect on the college gap, but a minor effect on segregation
  - ▶ The amenity externalities and the mobility costs have direct effects on segregation
  - ▶ Changes in segregation affect the exposure to high-quality neighborhoods and the college gap

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  - ▶ The amenity externalities and the mobility costs have direct effects on segregation
  - ▶ Changes in segregation affect the exposure to high-quality neighborhoods and the college gap
- ▶ Escaping segregation traps
  - ▶ Spillovers + amenity externalities  $\implies$  multiple equilibria
  - ▶ Economy can coordinate to live in a less segregated equilibrium

▷ Related literature

Model



## Model

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- ▶ Overlapping generations who each live 2 periods
- ▶ Households are of **race**  $r$  in  $\{B, W\}$  which impacts:
  - ▶ **Wages**: calibrated Black-White wage gap
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- ▶ 3 **neighborhoods**  $n$  in  $\{A, B, C\}$ , with 3 **equilibrium** characteristics:
  - ▶ Rent:  $p_n$
  - ▶ **Local spillover**:  $X_n$ , college share
  - ▶ **Racial composition**:  $S_{r,n}$ , population share of each race

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  - ▶ **Racial composition**:  $S_{r,n}$ , population share of each race
- ▶ Timing:
  - ▶ Adults choose their **neighborhood**
  - ▶ They decide how much to **consume** and **invest** in their child
  - ▶ The child is born, realization of ability and education preference shock
  - ▶ Child chooses **education level**,  $e$  in  $\{e^L, e^H\}$ , with which they will enter adulthood

## Adult Problem: Consumption, Investment, and Neighborhood Choices

$$V(r, a, s, e, n_0, n) = \max_{c, i} \log(c) + \log(A(n, r, S_{r,n})) + \beta \mathbb{E}_{e,a} [\mathcal{V}(r, a', s', e', n)]$$

subject to

$$c + i + p_n + m(r)\mathbb{I}(n \neq n_0) = y(r, e, s)$$

$$a' \sim \Gamma(a)$$

$$s' = F^s(a', i, X_n)$$

$$P(e' = e^H) = G^e(r, a', s', n)$$

- ▶ **Amenity externalities:** neighborhood valuation depends on racial composition,  $S_{r,n}$
- ▶ **Mobility cost:** depends on race
- ▶ **Income:** depends on race, education, and skills
- ▶ **Local spillover:** share of college-educated adults,  $X_n$

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- ▶ **Local spillover:** share of college-educated adults,  $X_n$
- ▶ Neighborhood choice:

$$\mathcal{V}(r, a, s, e, n_0) = \max_n \{V(r, a, s, e, n_0, n) + \varepsilon^n\}$$

$\varepsilon^n$ : neighborhood preference shock drawn from a type 1 extreme value distribution

## Child's Problem: Education Choice

- ▶ Skill formation:

$$\log s = \theta_c + \underbrace{\theta_a \log(a) + \theta_i \log(i)}_{\text{individual}} + \underbrace{\theta_x \log(X_n)}_{\text{neighborhood}}$$

- ▶ Skill affects: (i) income, (ii) education cost
- ▶ Education choice:

$$e = \operatorname{argmax}_{\{e^L, e^H\}} \{ \mathcal{V}(r, a, s, e^L, n) + \sigma^L, \mathcal{V}(r, a, s, e^H, n) - \underbrace{(\bar{c} - s)}_{\text{educ. cost}} + \sigma^H \}$$

- ▶  $\sigma^H, \sigma^L$  are preference shocks drawn from a type 1 extreme value distribution
- ▶ The cost of acquiring education is decreasing in skill

## Three General Equilibrium Forces

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- ▶ **Housing:** elastically supplied,  $S_n = \eta_n p_n^\psi$
- ▶ **Local spillovers:**  $X_n$ , share of adults with  $e^H$
- ▶ **Amenity externalities:**  $S_{r,n}$ , race shares by neighborhood

▷ Equilibrium Definition

Quantification



# Calibration Strategy

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Focus on St. Louis MSA

► **Five key empirical estimates:**

1. [Amenity externalities](#)
2. [Black-White wage gap](#)  
Race penalty of  $\approx 8\%$
3. [Moving across neighborhoods](#)  
Black households  $\approx 6$  p.p. less likely to move
4. [Neighborhoods](#)
5. [Skills and education](#)

} Sources of racial differences

► **Calibration:** some external and some internal, to match the data

► **Validation:** replicate 2 estimates of [causal effects](#) from the literature

▷ [Details wage gap](#)

▷ [Details moving across neighborhoods](#)

▷ [Details skill](#)

## Amenity Externalities

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Why do amenities depend on racial composition?

- ▶ Homophily, discrimination (Becker and Murphy, 2000)

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Model:

- ▶ Penalty on exogenous amenities (Banzhaf and Walsh, 2013):

$$A(n, r, S_{r,n}) = A_n (1 - \varphi_r (S_{r,n} - \gamma_r)^2)$$

- ▶ Utility from exogenous amenities  $A_n$  decreases as racial composition differs from ideal
- ▶  $S_{r,n}$  is the share of population of race  $r$  in  $n$
- ▶  $\gamma_r$  is the “bliss point” for racial composition,  $\varphi_r$  is a weight on the penalty

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Data:

- ▶ Survey evidence:  $\gamma_B = 0.5$ ,  $\gamma_W = 0.9$  (Farley et al., 1997; Krysan and Farley, 2002) ▶ [Details](#)
- ▶ Causal effect of racial composition on neighborhood choice (Caetano and Maheshri, 2021)  
Choose  $\varphi_r$  to target these causal effects ▶ [Details](#)

## Neighborhoods

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- ▶ Use a  $k$ -means clustering of Census tracts based on: (i) household income, (ii) house prices, (iii) share of adults with college degree, and (iv) Black share
- ▶ 3 neighborhoods:
  - ▶ A: Black (78%) and low-income (\$33k)
  - ▶ B: White (91%) and middle-income (\$55k)
  - ▶ C: White (93%) and high-income (\$85k)

▷ [Details](#)   ▷ [Map](#)

## Calibration: Internal Parameters and Targeted Moments

Parameter	Description	Value	Moment	Data	Model
Neighborhoods					
$A_A$	Amenity in A	1.0000	Population neighborhood A	0.1700	0.1743
$A_B$	Amenity in B	1.1178	Population neighborhood B	0.6200	0.6159
$A_C$	Amenity in C	1.2207	Population neighborhood C	0.2100	0.2098
$\eta_A$	Housing supply in A	25.3023	Rent neighborhood A	0.1200	0.1213
$\eta_B$	Housing supply in B	22.6165	Rent neighborhood B	0.2178	0.2172
$\eta_C$	Housing supply in C	1.4118	Rent neighborhood C	0.4460	0.4459
$\kappa$	Shape parameter for location	0.1492	Neighborhood flows	0.3500	0.4076
$m^B$	Migration cost for Black HHs	0.0595	Difference in moving prob for Black HHs	-0.0610	-0.0629

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$\varphi_W$	White	0.6541	Migration response to Black share, Black non-college	0.0241	0.0356
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<b>Skill</b>					
$\theta_c$	Constant term	0.5552	Mean skills	1.0000	1.2178
$\theta_a$	Ability	0.5471	Regression coefficient of education on skills	0.1910	0.1895
$\theta_i$	Investment	0.4529	Covariance ( $s, i$ )	0.1612	0.2199
$\theta_X$	Spillovers	0.1697	Ratio college share neighborhood C to A	3.5333	3.3946



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<b>Ability</b>					
$\rho_a$	Persistence ability	0.3984	Regression coefficient of child on parent ability	0.5100	0.5055
$\sigma_a$	Std. dev. ability	1.1881	$R^2$ child on parent ability	0.2600	0.2555
<b>Education</b>					
$\bar{c}$	Education cost level	2.1125	Educational probability	0.4166	0.4245
$\sigma$	Shape parameter education	0.4109	$R^2$ education choice	0.1570	0.1450

## Model Validations

### Validation 1: Moving to Opportunity (Chetty et al., 2016)

- ▶ **Data:** MTO voucher program increased college attainment
- ▶ **Model:** Subsidize rent differences across neighborhoods for households living in A

	Data	Model
Takeup rate (%)	[46.0, 49.3]	31.0
College attainment, treatment-on-the-treated (%)	[ 2.9, 7.6]	4.1
College attainment, intent-to-treat (%)	[ 1.4, 3.7]	1.3

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### Validation 2: Causal effect of segregation (Ananat, 2011)

- **Data:** Use train tracks instrument to measure causal effect of segregation on college attainment
- **Model:** Eliminate amenity externality, evaluate the response in college

	Data	Model
$\Delta$ college attainment, White	[-0.29, 0.012]	0.0791
$\Delta$ college attainment, Black	[-0.52, -0.078]	-0.2108

Model: Segregation and College Gap

## Model Explains Segregation and the College Gap

Model generates 80% of the college gap and the level of segregation

	Data	Model
<b>College attainment:</b>		
All, %	0.42	0.42
White, %	0.47	0.47
Black, %	0.19	0.25
College gap, p.p.	0.28	0.22
<b>Black share:</b>		
All	0.20	0.20
Neighborhood A	0.78	0.79
Neighborhood B	0.09	0.09
Neighborhood C	0.07	0.04
Dissimilarity Index	0.61	0.65

### Wage gap:

Higher earnings enable White HH to afford better neighborhoods, invest in kids

### Amenity externalities:

Drives White HHs to C and Black HHs to A  
Segregation  $\Rightarrow$  lower spillovers for Black  $\Rightarrow$  college gap

### Mobility cost differences:

Reinforces these outcomes

▷ Dissimilarity index

▷ Role of heterogeneity

Sources of College Gap: Wage Gap, Amenity Externality, Mobility Cost

## No Wage Gap Counterfactual, $w(B, e) = w(W, e)$

	GE change in			College gap	Dissimilarity index
	$X_n$	$S_{r,n}$	$p_n$		
<i>Benchmark</i>				0.22	0.65
<i>General equilibrium</i>	✓	✓	✓	0.06	0.46

- ▶ Removing the Black-White wage gap decreases segregation by 29% and college gap by 16 p.p.

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	$X_n$	$S_{r,n}$	$p_n$		
<i>Benchmark</i>				0.22	0.65
<i>General equilibrium</i>	✓	✓	✓	0.06	0.46
<i>Partial equilibrium</i>	×	×	×	0.17	0.60
<i>No <math>\Delta</math> spillovers</i>	×	✓	✓	0.16	0.61
<i>No <math>\Delta</math> race amenities</i>	✓	×	✓	0.13	0.59
<i>No <math>\Delta</math> rental price</i>	✓	✓	×	0.10	0.47

- ▶ Removing the **Black-White wage gap** decreases segregation by **29%** and college gap by **16 p.p.**
- ▶ Strong GE effects of change in **spillovers** for the college gap
- ▶ Strong GE effects of change in **spillovers and race amenities** for segregation

▷ Investment



## Race-Blind Counterfactual: No Amenity Externality, $\varphi_b = \varphi_w = 0$

---

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	$X_n$	$S_{r,n}$	$p_n$		
<i>Benchmark</i>				0.22	0.65
<i>General equilibrium</i>	✓	✓	✓	0.05	0.07

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<i>No <math>\Delta</math> rental price</i>	✓	✓	×	0.06	0.07

- ▶ Removing **amenity externality** decreases segregation by **89%** and college gap by **17 p.p.**
- ▶ GE effects are not important
- ▶ Changes in **segregation** affect the exposure to high-quality neighborhoods and the **college gap**

## Equal Mobility Cost

	GE change in			College gap	Dissimilarity index
	$X_n$	$S_{r,n}$	$p_n$		
<i>Benchmark</i>				0.22	0.65
<i>General equilibrium</i>	✓	✓	✓	0.12	0.28

- Equalizing mobility costs decreases segregation by 57% and college gap by 10 p.p.

► Effects on intergenerational mobility

## Equal Mobility Cost

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<i>Partial equilibrium</i>	×	×	×	0.22	0.59
<i>No <math>\Delta</math> spillovers</i>	×	✓	✓	0.16	0.40
<i>No <math>\Delta</math> race amenities</i>	✓	×	✓	0.22	0.60
<i>No <math>\Delta</math> rental price</i>	✓	✓	×	0.15	0.37

- ▶ Equalizing mobility costs decreases segregation by 57% and college gap by 10 p.p.
- ▶ Strong GE effects of spillovers and racial composition
- ▶ Changes in segregation affect the exposure to high-quality neighborhoods and the college gap

▷ Effects on intergenerational mobility

## Multiple Equilibrium

## Spillovers + Amenity Externality $\Rightarrow$ Multiple Equilibrium

---

	Equilibrium 1	Equilibrium 2
Dissimilarity index	0.65	0.42
College gap	0.22	0.10
SSE	0.03	1.27

### Equilibrium 1:

- ▶ Segregated equilibrium
- ▶ Matches the data

### Equilibrium 2:

- ▶ Integrated equilibrium
- ▶ Lower college gap

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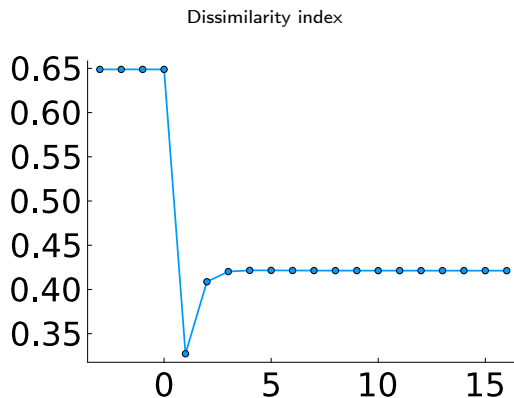
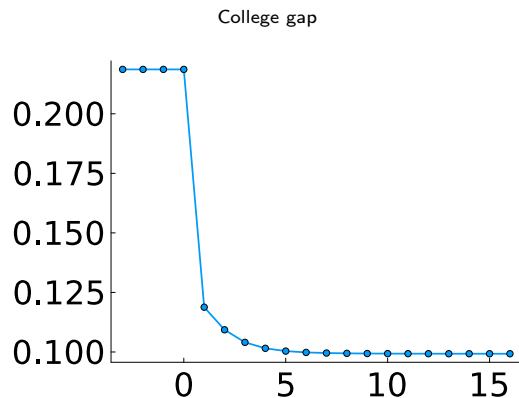
- ▶ Integrated equilibrium
- ▶ Lower college gap

Can we coordinate to move the economy from the segregated to the integrated equilibrium?

- ▶ Start in Equilibrium 1
- ▶ In period  $t = 0$  agents learn that in period  $t = \tau$  they will coordinate to be in Equilibrium 2
- ▶ What is the transition path?

▷ Third equilibrium

## Escaping the Segregation Trap



- ▶ Fast coordination to equilibrium 2, robust for different values of  $\tau$
- ▶ Lower college gap and segregation



## Conclusion

## Conclusion

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Add race to a benchmark model of a city with neighborhood spillovers

- ▶ Model replicates 80% of the Black-White college gap, and the level of segregation

### Takeaways:

1. Closing the Black-White wage gap alone does *not* completely reduce college gap or segregation
  - ▶ Neighborhood racial segregation largely maintained
2. Other way to reduce the gap: households move across neighborhoods, equalizing spillovers
  - ▶ Eliminating the amenity externality in preferences has the largest impact
  - ▶ Reduces segregation even though racial income and financial constraints remain in place
3. Multiple equilibria
  - ▶ The data indicate that St. Louis is in the segregated equilibrium
  - ▶ Exists a second, more integrated equilibrium with a lower college gap
  - ▶ A transition from the segregated to the integrated equilibrium can be fast

# Appendices

- ▶ **Empirical literature:**

- ▶ Ananat (2011); Biasi (2021); Billings et al. (2013); Boustan (2013); Cameron and Heckman (2001); Card and Rothstein (2007); Chetty and Hendren (2018a,b); Chetty et al. (2016); Cutler and Glaeser (1997); Derenoncourt (2022); Graham (2018); Hyman (2017); Jackson et al. (2016); Monarrez and Schönholzer (nd); Neal and Johnson (1996)

- ▶ **Racial segregation in spatial equilibrium, but no human capital:**

- ▶ Schelling (1969), Schelling (1971)
- ▶ Banzhaf and Walsh (2013), Bayer et al. (2004), Bayer and McMillan (2005), (Caetano and Maheshri, 2021)

- ▶ **Neighborhood spillovers in human capital accumulation, but no race:**

- ▶ Fernandez and Rogerson (1996), Brock and Durlauf (1995), Benabou (1996)
- ▶ Aliprantis and Carroll (2018), Fogli and Guerrieri (2019), Zheng and Graham (2022), Eckert and Kleineberg (2019), Chyn and Daruich (2022)

- ▶ **Our contribution:** Add race to a spatial model with education and neighborhood spillovers

- ▶ Badel (2015)

## Recursive Competitive Equilibrium

A *Recursive Competitive Equilibrium* is characterized by policy functions for the neighborhood choice  $n(r, a, s, e, n_0)$ , consumption  $c(r, a, s, e, n_0, n)$ , and investment  $i(r, a, s, e, n_0, n)$  decisions of the parent, the education choice  $e'(r, a, s, e, n)$  of the child, value functions  $V(r, a, s, e, n_0, n)$ , house prices  $\{p_n\}_{n=1}^N$ , local spillovers  $\{X_n\}_{n=1}^N$ , neighborhood racial shares  $\{S_{r,n}\}_{n=1}^N \forall r \in \{B, W\}$ , and an ergodic distribution  $F(r, a, s, e, n_0, n)$  over race, ability, skills, education, birth neighborhood, and adult neighborhood, which satisfy the following:

1. Household optimization: the policy functions  $n, e', c, i$  solve both the adult's and child's problem.
2. Housing market clearing:

$$\eta_n p_n^\psi = S_n = \int F(dr, da, ds, de, dn_0, n) \quad \forall n = 1, \dots, N$$

3. Spillover consistency:

$$X_n = \frac{\int F(dr, da, ds, e^H, dn_0, n)}{\int F(dr, da, ds, de, dn_0, n)} \quad \forall n = 1, \dots, N$$

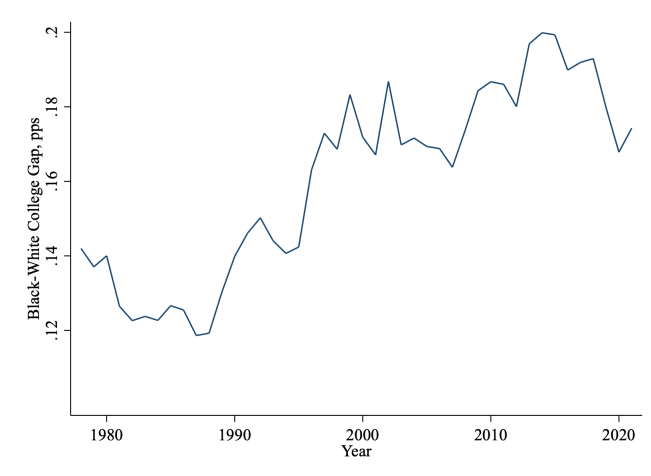
4. Location consistency:

$$S_{r,n} = \frac{\int F(r, da, ds, de, dn_0, n)}{\int F(dr, da, ds, de, dn_0, n)} \quad \forall n = 1, \dots, N \text{ and } r = \{b, w\}.$$

Data

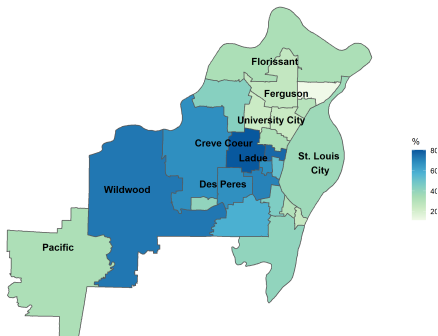
## Black-White College Attainment Gap

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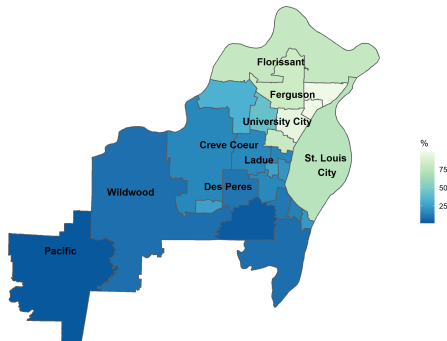


## High Correlation between Race and College Attainment in St. Louis

College Enrollment



Black Share



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## Survey Evidence

Survey evidence from (Farley et al., 1997; Krysan and Farley, 2002)

Attractiveness Ratings of Neighborhoods  
by Racial Composition (Black Respondents)

All Black	20%
Majority Black	23%
50% Black	50%
Majority White	5%
All White	2%

Reasons Blacks Find  
A Neighborhood Most Attractive

Because it is mixed	56%
Positive effects of integration	22%
Better neighborhood characteristics	7%
White hostility	4%
Other	11%

Krysan and Farley (2002)

**TABLE 1: Attractiveness Ratings of Neighborhoods by Racial Composition and Rank Order (Black Respondents)**

	First Choice	Second Choice	Third Choice	Fourth Choice	Fifth Choice
	Percent	Percent	Percent	Percent	Percent
All black	20	7	24	32	16
10 black–4 white	23	58	13	6	1
7 black–7 white	50	22	26	1	< 1
2 black–12 white	5	12	34	49	1
All white	2	2	3	12	81
Total	100	100	100	100	100
Sample size	2001	1995	1989	1977	1975

## Estimating the Causal Effect of Race

(Caetano and Maheshri, 2021): Model of neighborhood choice isolating the causal effect of race from other neighborhood characteristics

	White		Black	
	Rich	Poor	Rich	Poor
Response to:				
Black Share	-2.83*** (0.40)	-2.25*** (0.45)	3.45*** (0.43)	2.41*** (0.42)
Poor Share	-0.69*** (0.24)	3.60*** (0.42)	-2.35*** (0.37)	0.44 (0.29)

Source: (Caetano and Maheshri, 2021)

- ▶ For White households, probability of choosing a neighborhood declines 2.25 or 2.83 percent when the Black share increases by 10 percentage points, for poor and rich households respectively
- ▶ Responses to race are larger than responses for income (except for poor White)
- ▶ Other papers find similar effects of race Bayer et al. (2017); Bayer and McMillan (2005); Bayer et al. (2004); Boustan (2013); Card et al. (2008)
- ▶ Validate our model comparing [causal effect of race](#) with (Caetano and Maheshri, 2021)

## Black-White Wage Gap

Mincer regression in NLSY-97:

$$\log(\text{earnings}_i) = \alpha \text{ race}_i + \beta \text{ college}_i + \underbrace{\chi \log(\text{ASVAB}_i)}_{\text{skill}} + \delta \text{ gender}_i + \varepsilon_i$$

Implies  $y(r, e, s) = w(r, e)s^\chi$

	Wage
<hr/>	
<i>Below college</i>	
White	1.00
Black	0.92
<hr/>	
<i>College or above</i>	
White	1.71
Black	1.58
<hr/>	
<i>Return to skill</i>	
$\chi$	0.185
<hr/>	

Gaps consistent with the literature (Heckman et al., 2006; Neal and Johnson, 1996)

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## Black-White Wage Gap Across Decades, St. Louis

	1980-1989	1990-1999	2000-2009	2010-2019
<i>Below college</i>				
White	1.000	1.000	1.000	1.000
Black	0.783	0.831	0.875	0.819
<i>College or above</i>				
White	1.281	1.567	1.632	1.817
Black	1.004	1.302	1.427	1.489

## Black-White Wage Gap Across Decades, National:

	1980-1989	1990-1999	2000-2009	2010-2019
<i>Below college</i>				
White	1.000	1.000	1.000	1.000
Black	0.823	0.893	0.910	0.895
<i>College or above</i>				
White	1.446	1.704	1.802	1.988
Black	1.190	1.522	1.639	1.729

## Moving Across Neighborhoods

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- ▶ Differential moving costs to capture a range of forces including:
  - ▶ Differences in borrowing constraints
  - ▶ Discrimination in housing markets
  - ▶ Information frictions
- ▶ Target: Racial difference in the intergenerational neighborhood moving probability controlling for:
  - ▶ Childhood household income
  - ▶ Parents education
  - ▶ Childhood neighborhood type
- ▶ Black households  $\approx 6$  p.p. less likely to move across neighborhood types

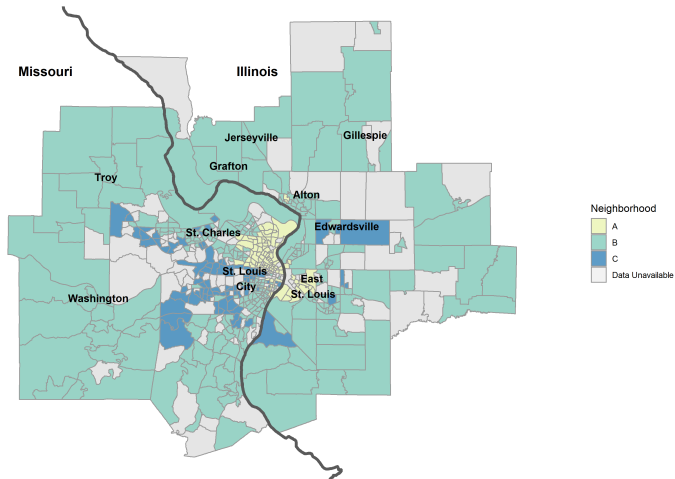
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## Mobility Difference for Black Households

Dependent variable: indicator for parent neighborhood type  $\neq$  child neighborhood type

	(1)
Childhood neighborhood type	
B	−0.328*** (0.026)
C	−0.188*** (0.029)
Log income	0.003 (0.009)
Race	−0.061** (0.028)
Constant	0.681*** (0.102)
<i>N</i>	3848
<i>R</i> <sup>2</sup>	.047
FE for parents' education	✓

# Neighborhood Segregation



## Clusters:

A: Black & low-income

B: White & middle-income

C: White & high-income



## Neighborhood Segregation

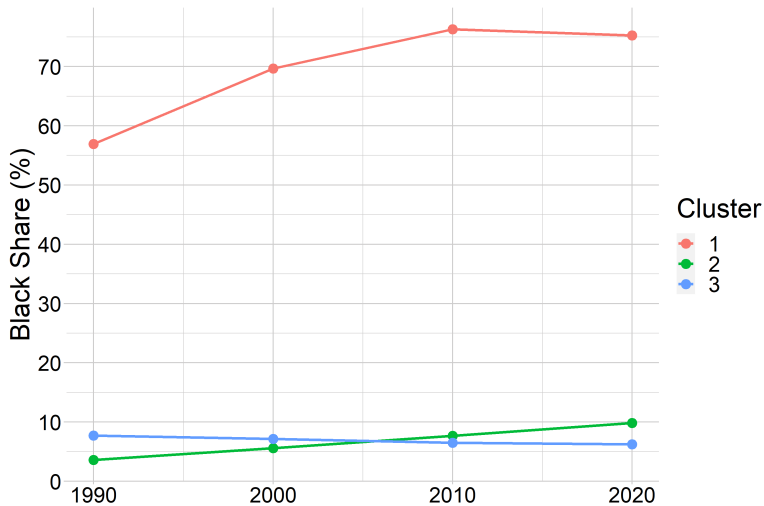
	All	Cluster A	Cluster B	Cluster C
Population Share	1.00	0.17	0.62	0.21
Black Share	0.20	0.78	0.09	0.07
College Share of Adults	0.28	0.15	0.23	0.53
Income (\$)	57,835	33,273	55,405	84,749
Median House Price (\$)	171,749	82,699	150,060	307,244

Notes: K-means clustering for St. Louis MSA. Data from 2000 Census and (Chetty et al., 2018)

- ▶ Cluster A: Majority Black & low-income
- ▶ Cluster B: Majority White & middle-income
- ▶ Cluster C: Majority White & high-income

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## Black Share by Cluster Over Time



## Skills and Education

### Model:

- ▶ Education cost depends on skill,  $s$
- ▶  $\log s = \theta_s + \underbrace{\theta_a \log(a) + \theta_i \log(i)}_{\text{individual}} + \underbrace{\theta_x \log(X_n)}_{\text{neighborhood}}$

### Target moments:

1. Importance of skill for education:  $\text{educ}_i = \alpha + \beta s_i + \varepsilon_i$
2. Importance of parental investment:  $\text{covariance}(s, i)$
3. Spillovers: Ratio college share neighborhood C to A,  $\frac{X_C}{X_A}$

Map between model and data from NLSY-97 and Census:

Model	Data
$s$ = skill	ASVAB score
$a$ = ability	unobserved
$i$ = investment	parental transfers
$X_n$ = neighborhood college share	neighborhood college share

## Calibration: External Parameters

Parameter	Description	Value	Source
$\beta$	Discount factor	0.97 <sup>40</sup>	
$\gamma_B$	Bliss points for Black households	0.50	Banzhaf and Walsh (2013)
$\gamma_W$	Bliss points for White households	0.90	Banzhaf and Walsh (2013)
$w(B, L)$	Relative wage of Black, low education	0.92	Mincer regressions
$w(B, H)$	Relative wage of Black, high education	1.58	Mincer regressions
$w(W, H)$	Relative wage of White, high education	1.71	Mincer regressions
$\psi$	Housing supply elasticity	2.36	Saiz (2010)
$m$	Moving cost, money	0.0033	Bergman et. al. (2019)

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## Neighborhood Flows

- ▶ Cluster Census tracts at the national level
  - ▶ K-means clustering algorithm on race share, income, housing prices, and college share
- ▶ NLSY: See county, race, education → estimate the probability of being in each cluster
- ▶ Compute the probability of moving between clusters between age 17 and 35.
- ▶ Conclusion: take a midpoint of 35% move across clusters

	Sample Restriction	
	50%	75%
Neighborhood flows	.461	.253
Observations	16,364	3,173

## Dissimilarity Index

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- ▶ Use dissimilarity index as in Ananat (2011)
- ▶ Dissimilarity index is defined as:

$$\text{seg} = \frac{1}{2} \sum_i^N \left| \frac{Black_i}{Black_{total}} - \frac{White_i}{White_{total}} \right|$$

where N is the number of neighborhoods

- ▶ Measures (Ananat, 2011):  
*“What percent of Blacks (or non-Blacks) would have to move to a different census tract in order for the proportion of Black households in each neighborhood to equal the proportion Black in the city as a whole?”*

## Quantitative Results

## Neighborhood Heterogeneity Matters

- ▶ Three GE neighborhood variables: **Spillovers** ( $X_n$ ), **race shares** ( $S_{r,n}$ ), and **rents** ( $p_n$ )
- ▶ What would happen if these are determined at the city, instead of neighborhood, level?

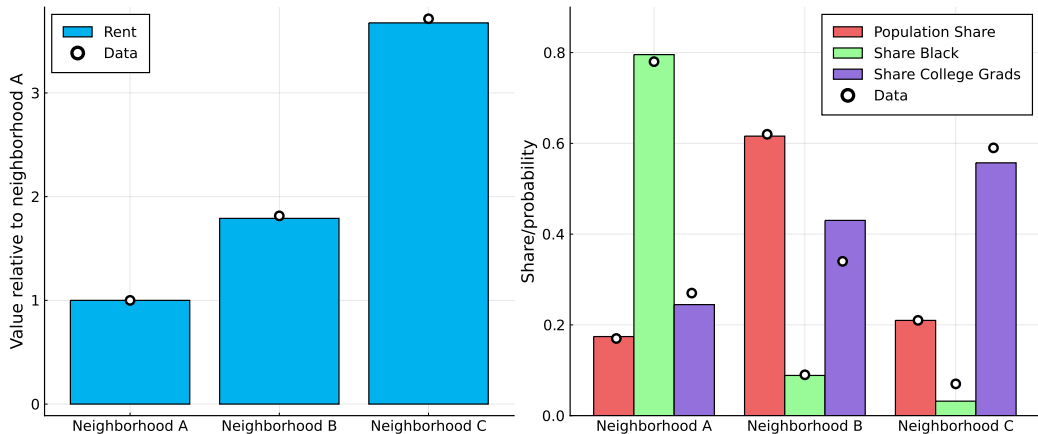
	College gap	Dissimilarity Index
Benchmark	0.22	0.65
Equal spillovers	0.08	0.57
Equal race shares	0.05	0.07
Equal rents	0.04	0.36

- ▶ Equal **spillovers**  $\implies$  lower college gap, but still high segregation
- ▶ Equal **race shares** or **rents**  $\implies$  lower segregation  $\implies$  lower college gap

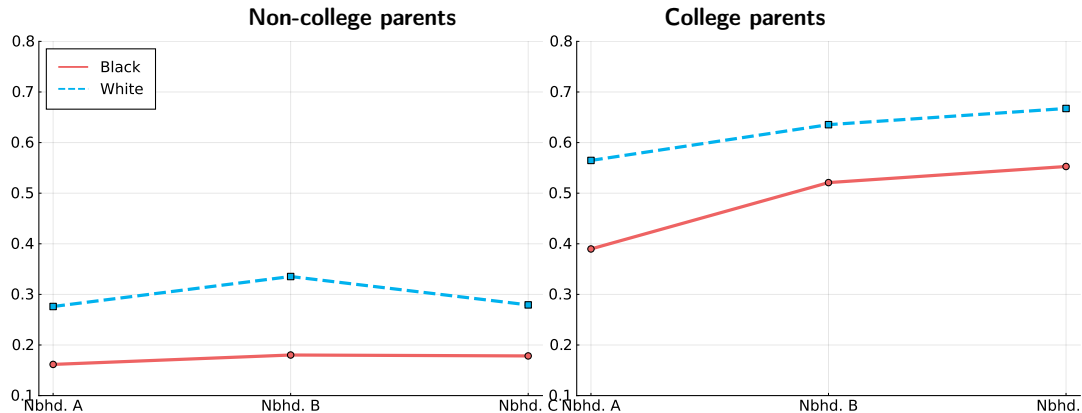
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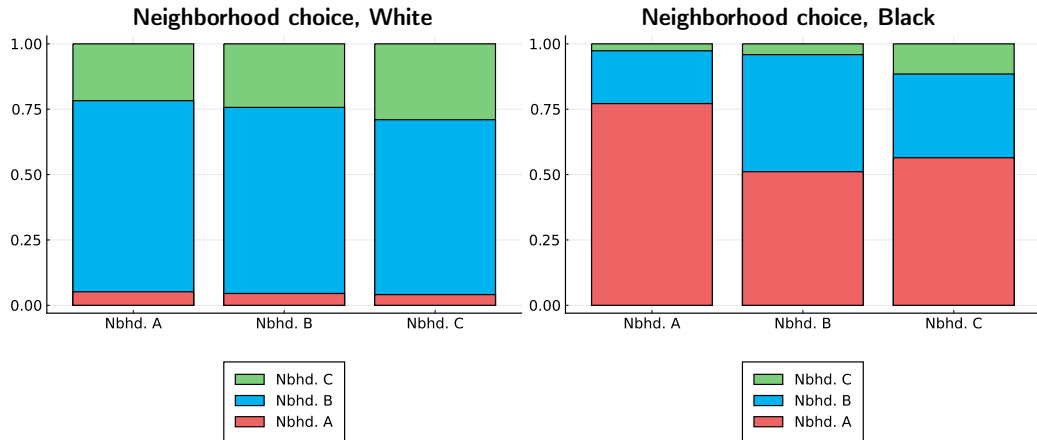
## Baseline: Neighborhood Characteristics



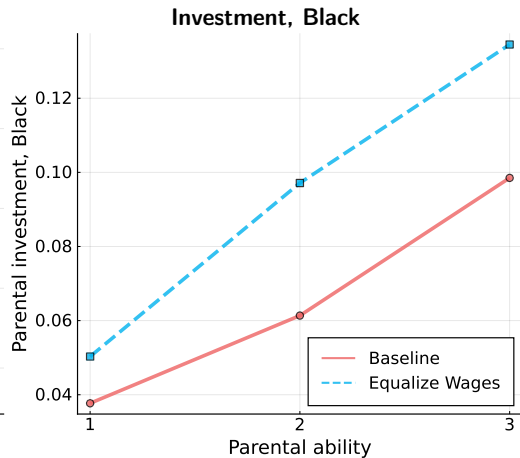
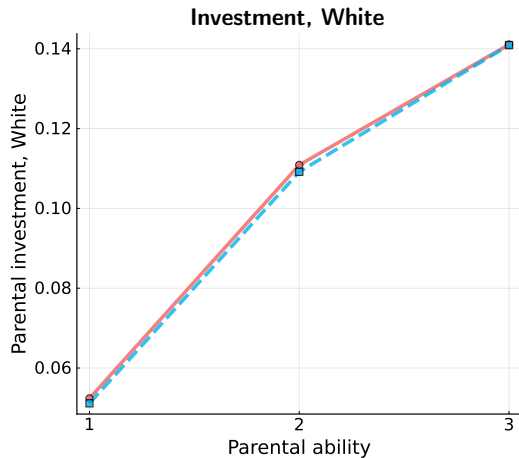
## Benchmark: Probability of Going to College



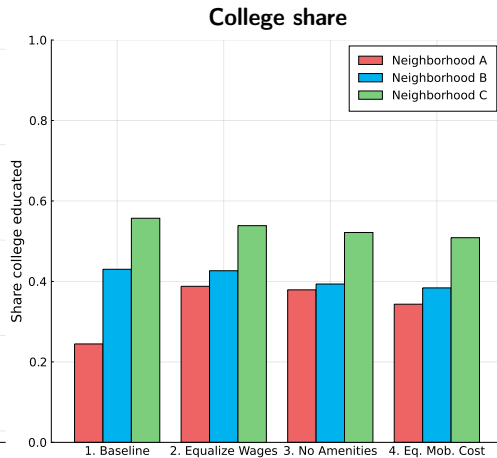
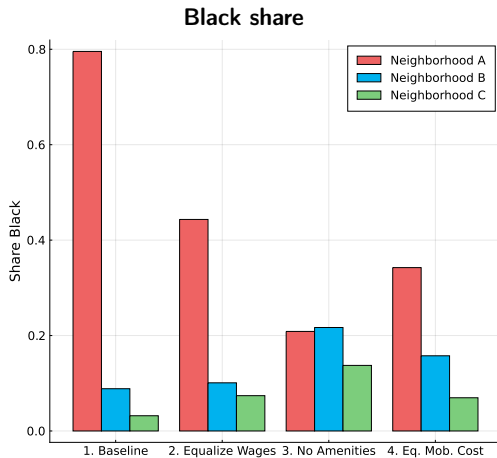
## Benchmark: Policy Rules, Neighborhood Choice



## Equalizing Wages: Investment is the Primary Driver of the Closing Education Gap



## Neighborhood Characteristics Equalization



### Improvements in intergenerational mobility among Black children

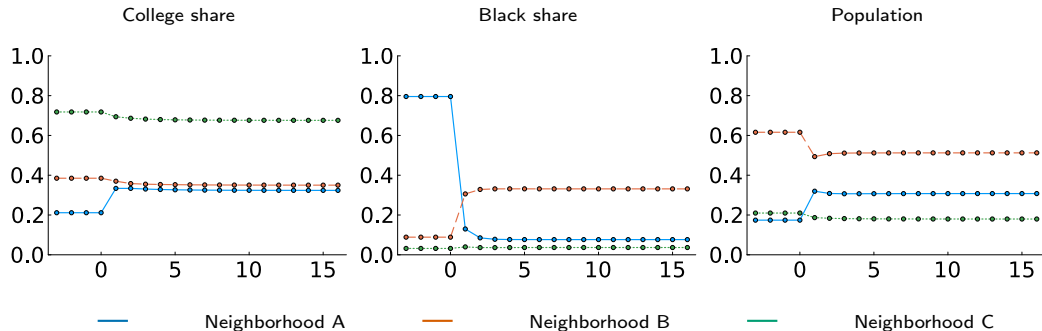
	Education Probability			
	Benchmark	No wage gap	Race blind	Equal mobility cost
Non-college parent, White	0.32	0.30	0.29	0.28
Non-college parent, Black	0.17	0.26	0.25	0.20
Gap	0.14	0.04	0.04	0.08
College parent, White	0.64	0.63	0.61	0.61
College parent, Black	0.48	0.58	0.58	0.52
Gap	0.17	0.04	0.03	0.09

## Third Equilibrium

---

- ▶ Almost everyone lives in C (except a few moves due to the EV shocks)
- ▶ As a result, the racial composition of C is close to 80% white, 20% black
- ▶ The racial composition of A and B is close to 100
- ▶ The value of the amenities of both A and B are very low for White and Blacks.
- ▶ As a result, they choose to stay in C, justifying the equilibrium.
- ▶ In other words, the housing supply elasticity, which pin down rents, is not enough to make everyone living in C not that attractive.
- ▶ But living in C is too expensive, so they do not become educated (education probability 1% due to EV shocks)

## Escaping the Segregation Trap



- Fast coordination to equilibrium 2, robust for different values of  $\tau$

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